# Position Tracking for Virtual Reality Using Commodity WiFi

#### [CVPR '17] Position Tracking for Virtual Reality Using Commodity WiFi

#### Motivation:

 Making VR free of dedicated infrastructure (IR cameras and sensors)

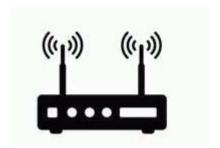
#### Contribution:

- Works even under occlusion
- Higher range
- Ubiquity and ease of deployment



## How is it done?

Replace IR cameras with wifi APs

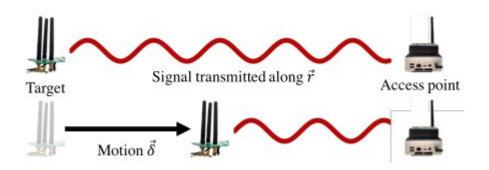




Replace IR sensors on the headset with a WiFi transmitter

#### Basic idea:

Change in path length causes change in phase.



If we can detect the change in phase, we can track the position. But there is Multipath

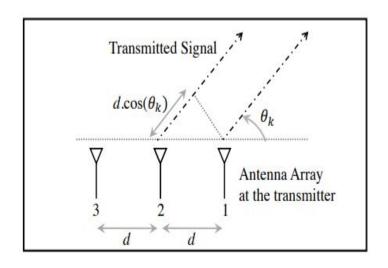
# Handling Multipath

- Use Antenna array at the transmitter
- Consider L paths

$$\mathbf{H} = [\vec{a}(\theta_1) \dots \vec{a}(\theta_L)]\mathbf{F} = \mathbf{AF}$$

H: Channel matrix

F: vector of weights of L paths



$$\vec{a}(\theta_k) = [1 e^{-j2\pi d \cos(\theta_k)/\lambda} e^{-j4\pi d \cos(\theta_k)/\lambda}]^{\top}.$$

### **CSI** calculation:

$$\hat{h}_q = \frac{1}{T} \int_0^T h_q e^{j2\pi f t} e^{-j2\pi f t + j\nu} dt = h_q e^{j\nu},$$

Phase offset between carriers at the AP and the transmitter.

So, Observed channel matrix is  $\hat{\mathbf{H}} = \mathbf{H}e^{j\nu}$ .

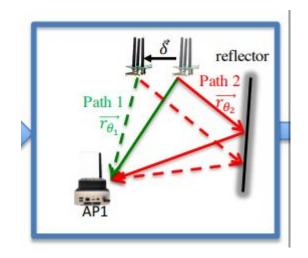
CSI measurements are done at the beginning of every WiFi packet.

# Change in channel due to Displacement

• Each path incurs a phase change  $e^{-j2\pi(\vec{r}_{\theta_k}^{\top}\cdot\vec{\delta})/\lambda}$ 

Channel matrix changes to

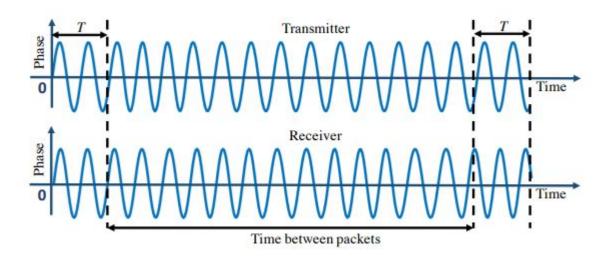
$$\mathbf{H}_2 = \mathbf{ADF},$$



$$\mathbb{C}^{L\times L} \text{ is a diagonal matrix with entries } \mathrm{e}^{-j2\pi(\vec{r}_{\theta_1}^\top \cdot \vec{\delta})/\lambda}, \ldots,$$
$$\mathrm{e}^{-j2\pi(\vec{r}_{\theta_{L-1}}^\top \cdot \vec{\delta})/\lambda}, \text{ and } \mathrm{e}^{-j2\pi(\vec{r}_{\theta_L}^\top \cdot \vec{\delta})/\lambda}.$$

# Phase distortion due to Frequency offset

Consider two consecutive wifi packets



$$\widehat{\mathbf{H}}_1 = \mathbf{A}\mathbf{F}e^{j\nu_1}, \widehat{\mathbf{H}}_2 = \mathbf{A}\mathbf{D}\mathbf{F}e^{j\nu_2}.$$

The phase offset can be so huge compared to the change in phase due to the displacement.

It is random too!

## Estimate AoD of all paths

Remember 
$$\mathbf{H} = [\vec{a}(\theta_1) \dots \vec{a}(\theta_L)]\mathbf{F} = \mathbf{AF},$$

To estimate steering vectors from single CSI measurement is impossible!

Collect CSI for P consecutive packets 
$$\mathbf{X} = [\hat{\mathbf{H}}_1 \ \hat{\mathbf{H}}_2 \ \dots \ \hat{\mathbf{H}}_P] = \mathbf{AG},$$

Apply **MUSIC** to find the steering vectors.

$$\widehat{\mathbf{F}}_p = \mathbf{A}^{\dagger} \widehat{\mathbf{H}}_p.$$

$$\widehat{\mathbf{F}}_1 = \mathbf{F} \mathrm{e}^{j\nu_1}, \widehat{\mathbf{F}}_2 = \mathbf{D} \mathbf{F} \mathrm{e}^{j\nu_2}$$

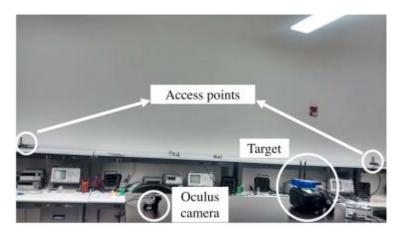
# Estimating the displacement during Packet duration

minimize 
$$\|\widehat{\mathbf{F}}_2 - \mathbf{D}\widehat{\mathbf{F}}_1\|$$
 subject to  $\mathbf{D}$  is diagonal.

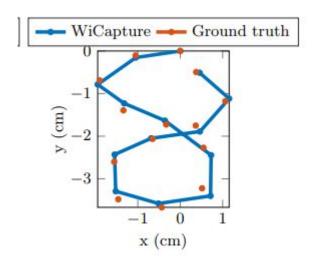
Note that  $\mathbf{D}_{k,k}$ , is an estimate of  $e^{-j2\pi(\vec{r}_{\theta_k}^\top \cdot \vec{\delta})/\lambda + j\nu_2 - j\nu_1}$ 

- All the diagonal elements contain the same random phase offset term
- •

## Results



(a) Indoor office deployment



## Comments:

How do we get a vector of CSI measurements at the APs?